

Meta-analysis of individual participant data from observational studies

Simon Thompson
University of Cambridge, UK

3. Risk prediction metrics



Freiburg, March 2013

Purpose

- Combine information on predictive ability of risk models across studies
- Assess how much a new risk marker aids risk prediction

Rationale

- Greater precision
- Reduced over-fitting
- Increased generalizability

Risk prediction models for multiple prospective studies

Cox proportional hazards model, stratified by study (s) and sex (k)

$$\log(h_{ski}(t | X)) = \log(h_{0sk}(t)) + \sum_p \beta_p X_{psi}$$

1-stage approach; ignores heterogeneity of β_p across studies

- focus is on estimates rather than their uncertainty
- easier to get absolute risk predictions than from a 2-stage random effects approach

Risk score = $\sum_p \hat{\beta}_p X_{psi}$ for individual i in study s

Risk discrimination in a single prospective study (i)

Harrell's C-index = probability that the predicted order of events is correct in a randomly selected pair of participants

$C = n_c / (n_c + n_d)$ where

n_c = # concordant pairs; n_d = # discordant pairs

C ranges from 0.5 to 1.0

The risk score is sufficient when ranking predicted risk

ΔC = change in C on adding a new risk marker

Variance of C and ΔC calculated by efficient jackknife estimator

Risk discrimination in a single prospective study (ii)

Royston-Sauerbrei's D statistic

- quantifies the association between ranked predicted risk and observed risk
- interpreted as log hazard ratio comparing top to bottom halves of predicted risks

D ranges from 0 upwards

ΔD = change in D on adding a new risk marker

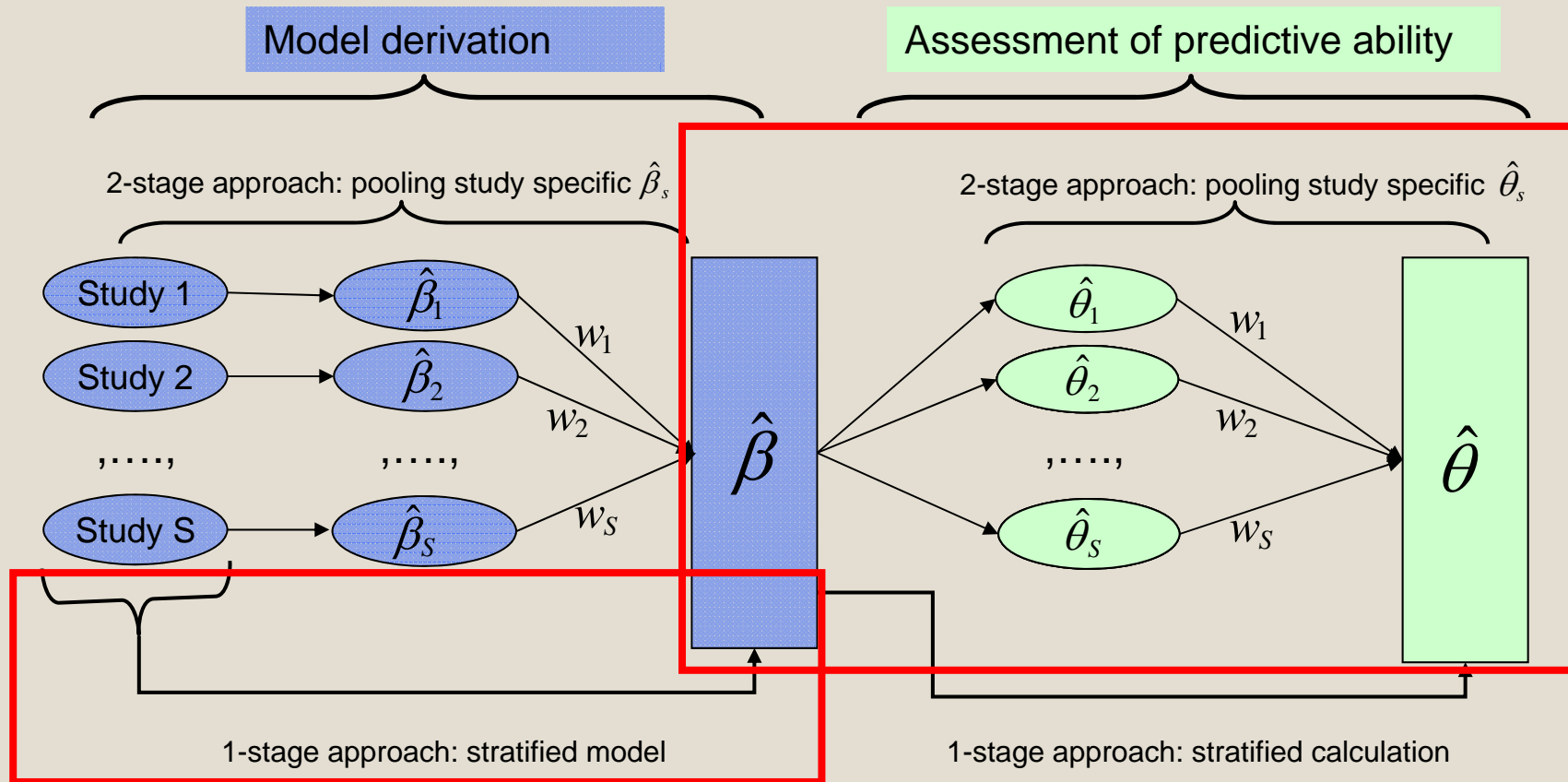
Variance of D obtained directly

Variance of ΔD obtained by bootstrapping

Stratified versions of C-index and D can be calculated

- e.g. stratifying by sex

Overall scheme for modelling and assessment



w_i = study-specific weights for meta-analysis

$\hat{\theta}_s$ = C, D, ΔC , or ΔD

Primary ERFC prediction analyses

Choice of weights in meta-analysis (1 & 2)

1. Inverse-variance (fixed effect)
2. Inverse-variance (random effects)

Meta-analysis of C-index and D

C_1 for model 1, C_2 for model 2, ΔC for difference

D_1 for model 1, D_2 for model 2, ΔD for difference

Inverse-variance weights leads to inconsistency between
pooled estimates of $C_2 - C_1$ and ΔC
pooled estimates of $D_2 - D_1$ and ΔD

Choice of weights in meta-analysis (3 & 4)

3. Number of events

Well matched to intrinsic weighting in stratified Cox PH model

4. Estimators stratified by study

For D, equivalent to option 3

For C, weights depend on number of informative pairs – large studies can receive substantial weight despite few events

Prefer option 3

Example

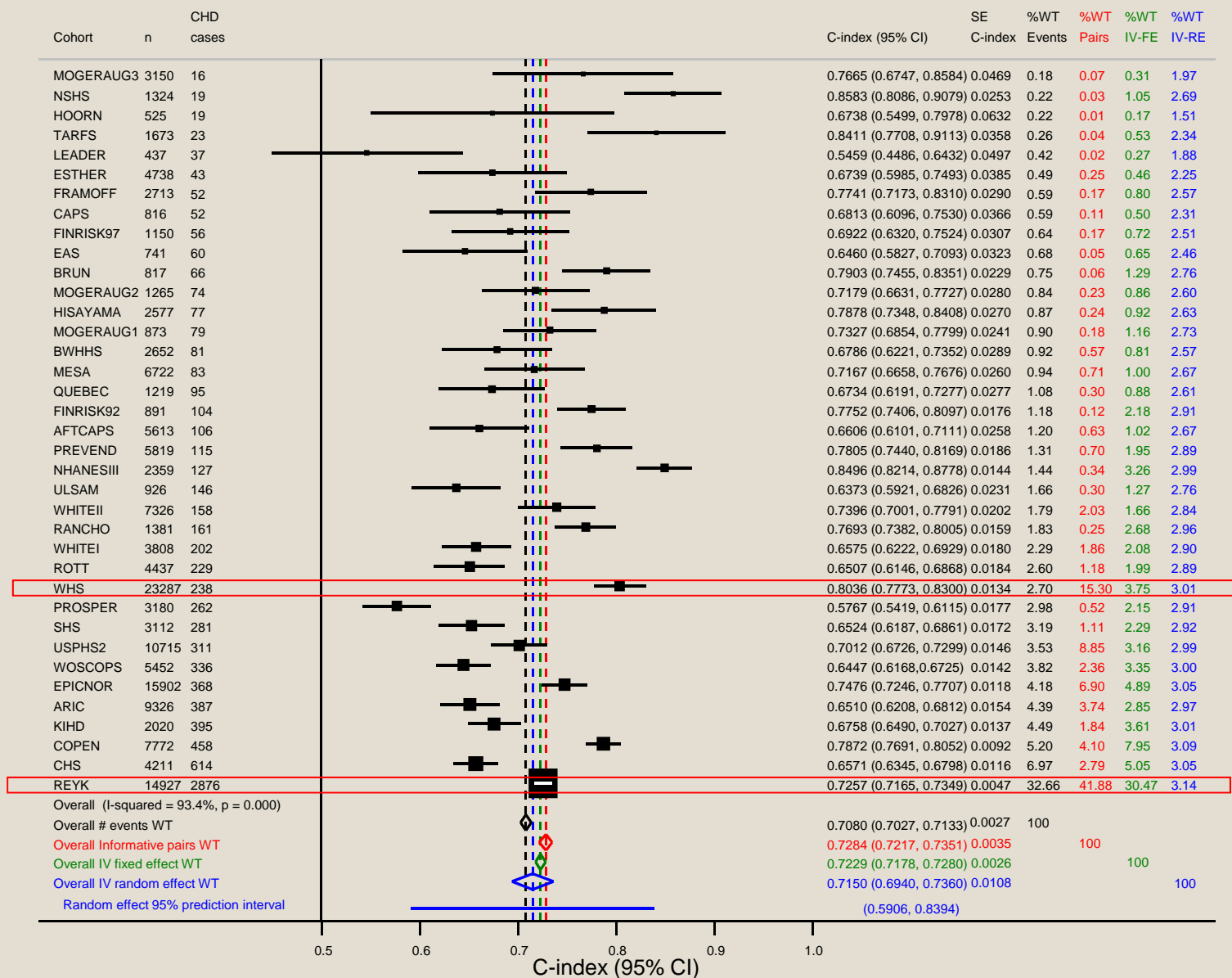
Prediction of CHD (fatal and non-fatal)

37 population-based prospective studies, 8806 CHD cases

Conventional risk factors: age, sex, smoking, systolic BP, diabetes, total chol, HDL chol

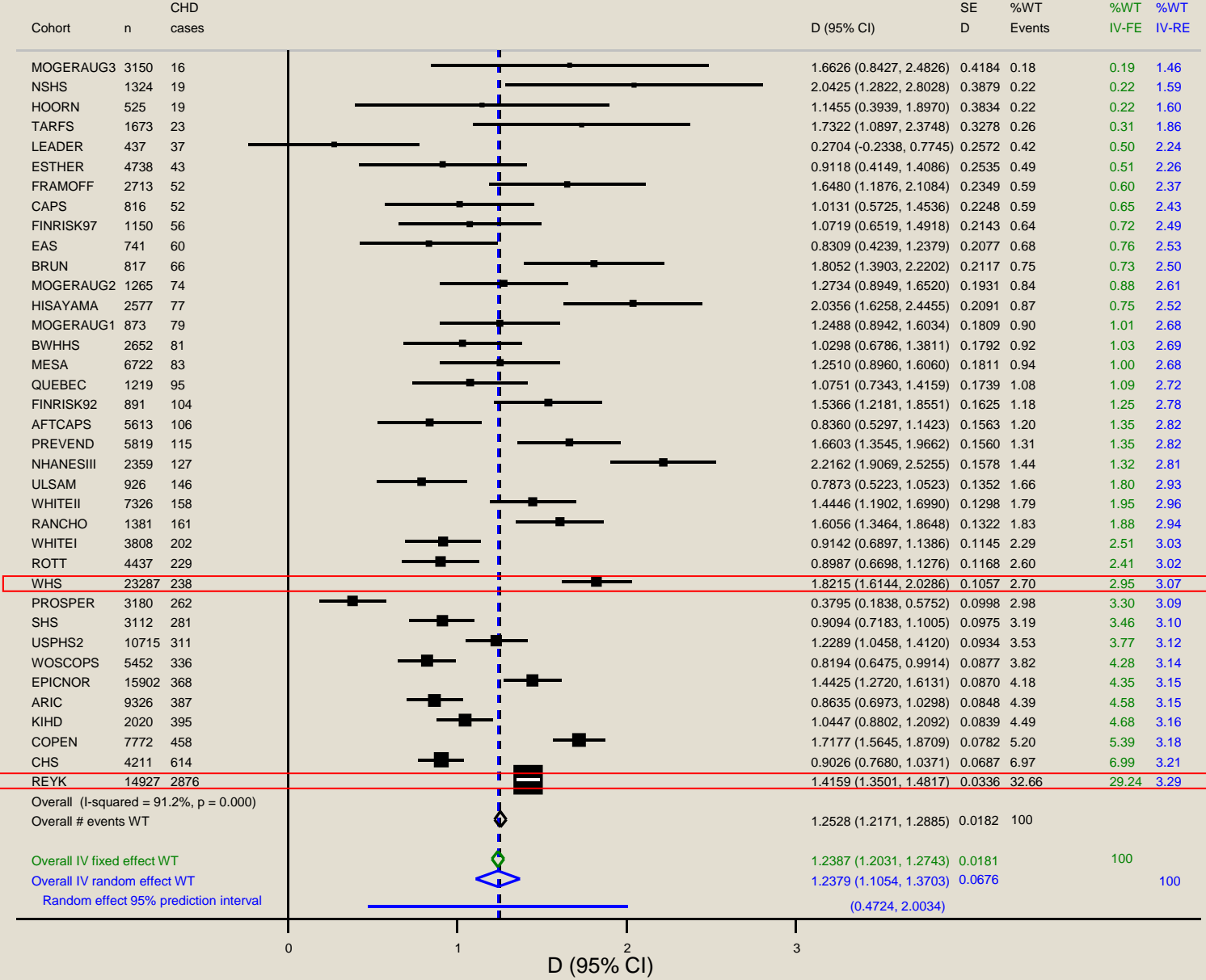
Investigate value of adding of log C-reactive protein (CRP), an inflammatory marker

Meta-analysis of C-index



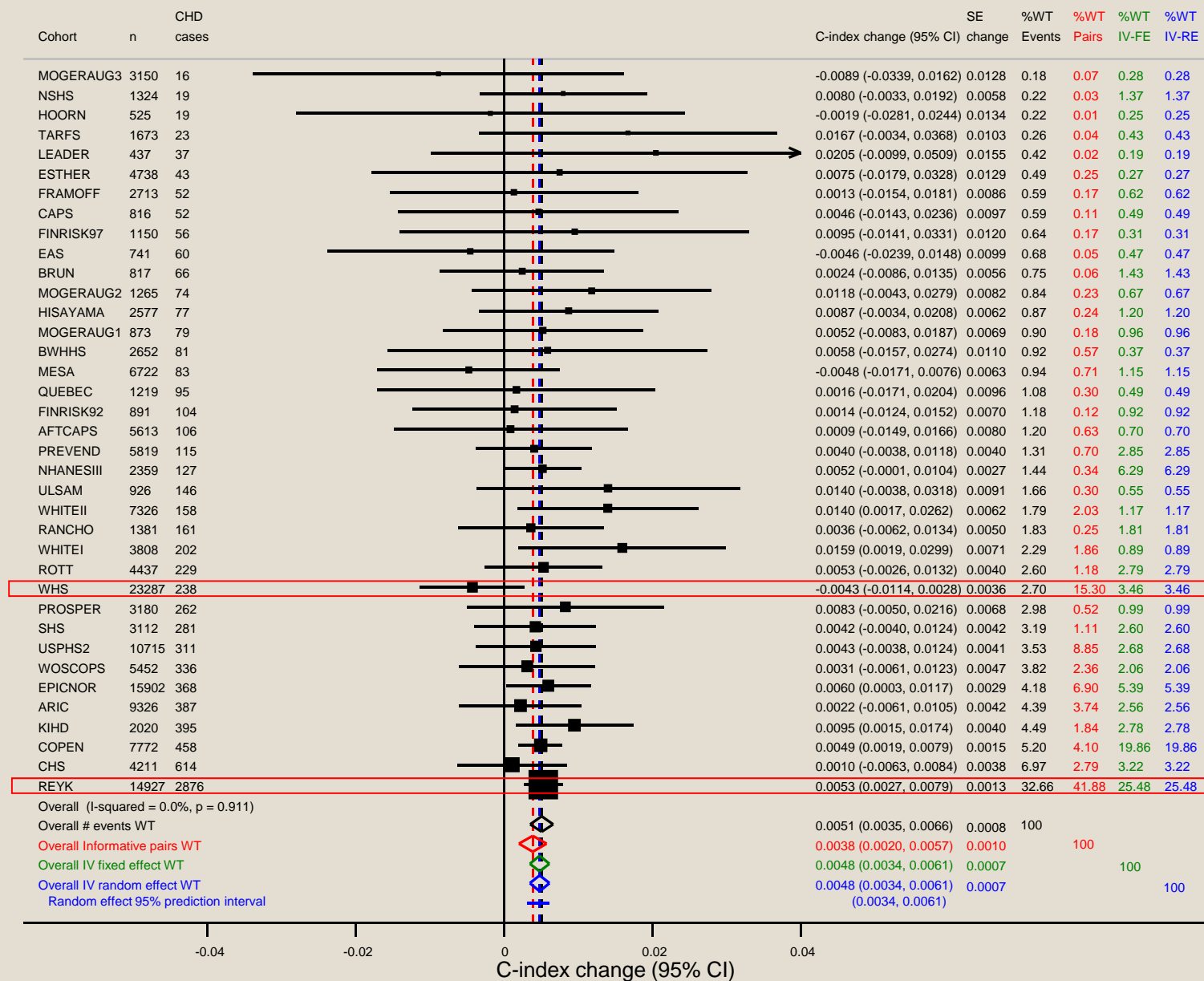
C-index with conventional CHD risk factors: age (sex), smoking, systolic BP, diabetes, total chol, HDL chol

Meta-analysis of D



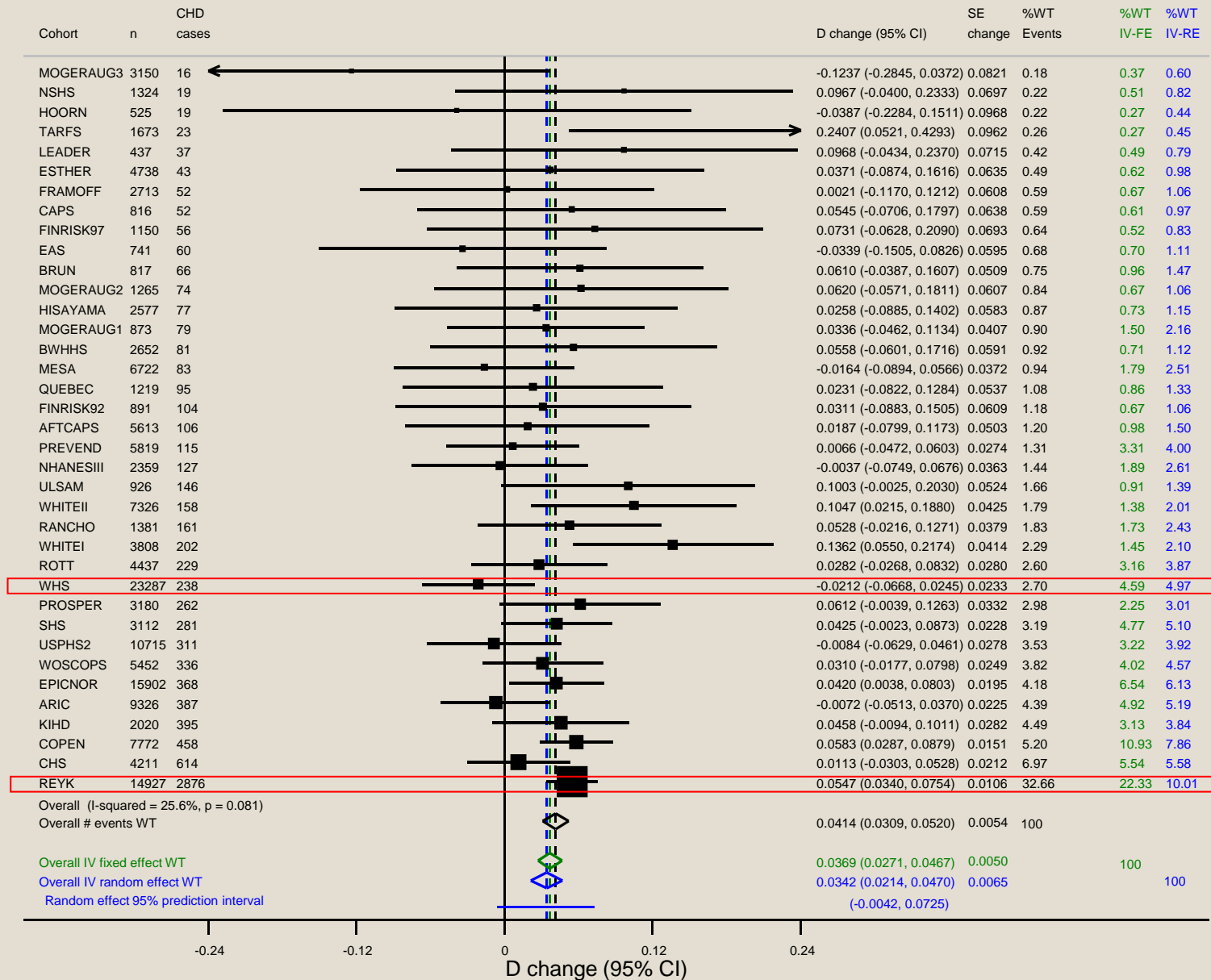
D with conventional CHD risk factors: age (sex), smoking, systolic BP, diabetes, total chol, HDL chol

Meta-analysis of C-index change



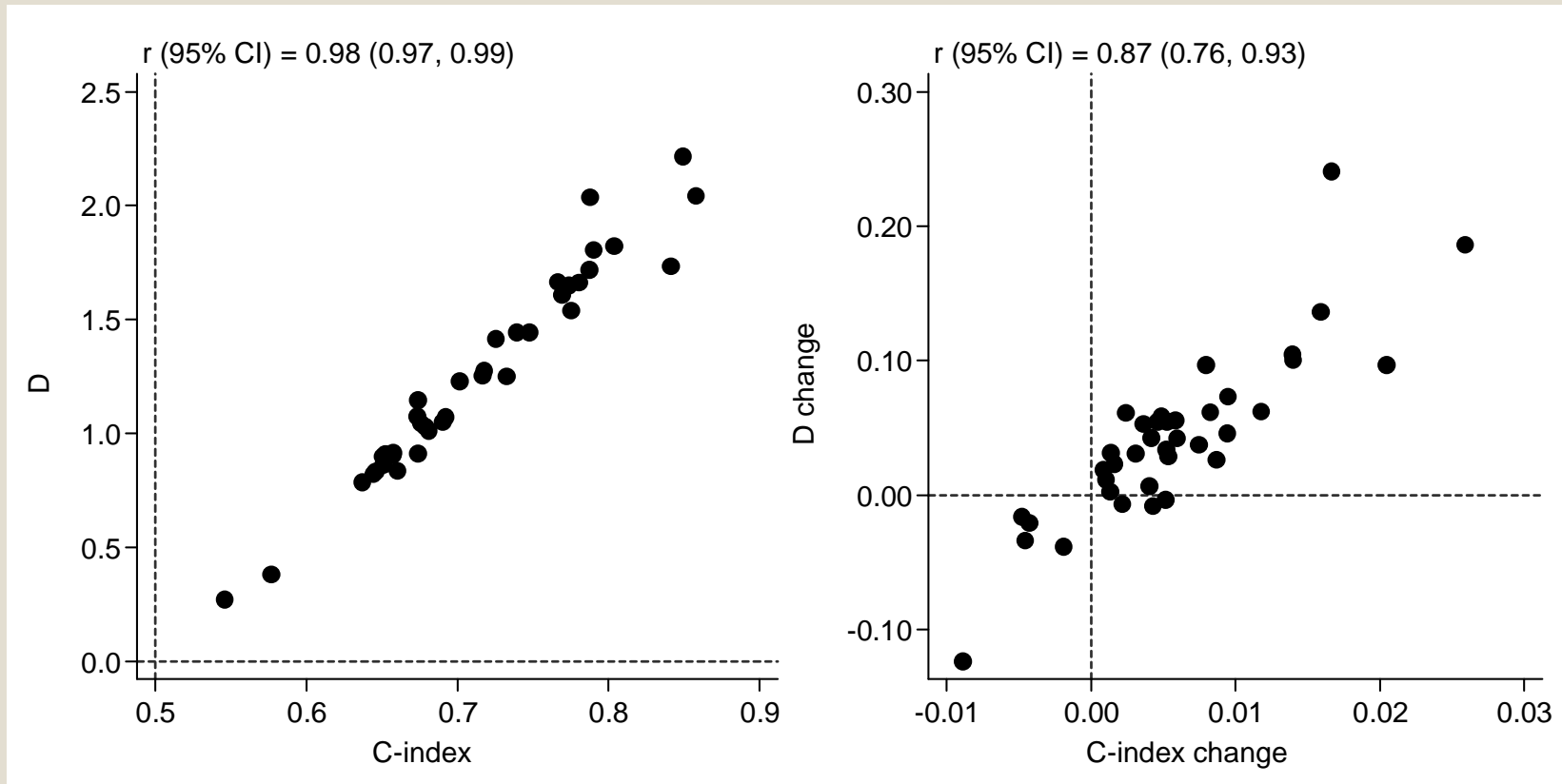
C-index change with addition of log CRP

Meta-analysis of D change

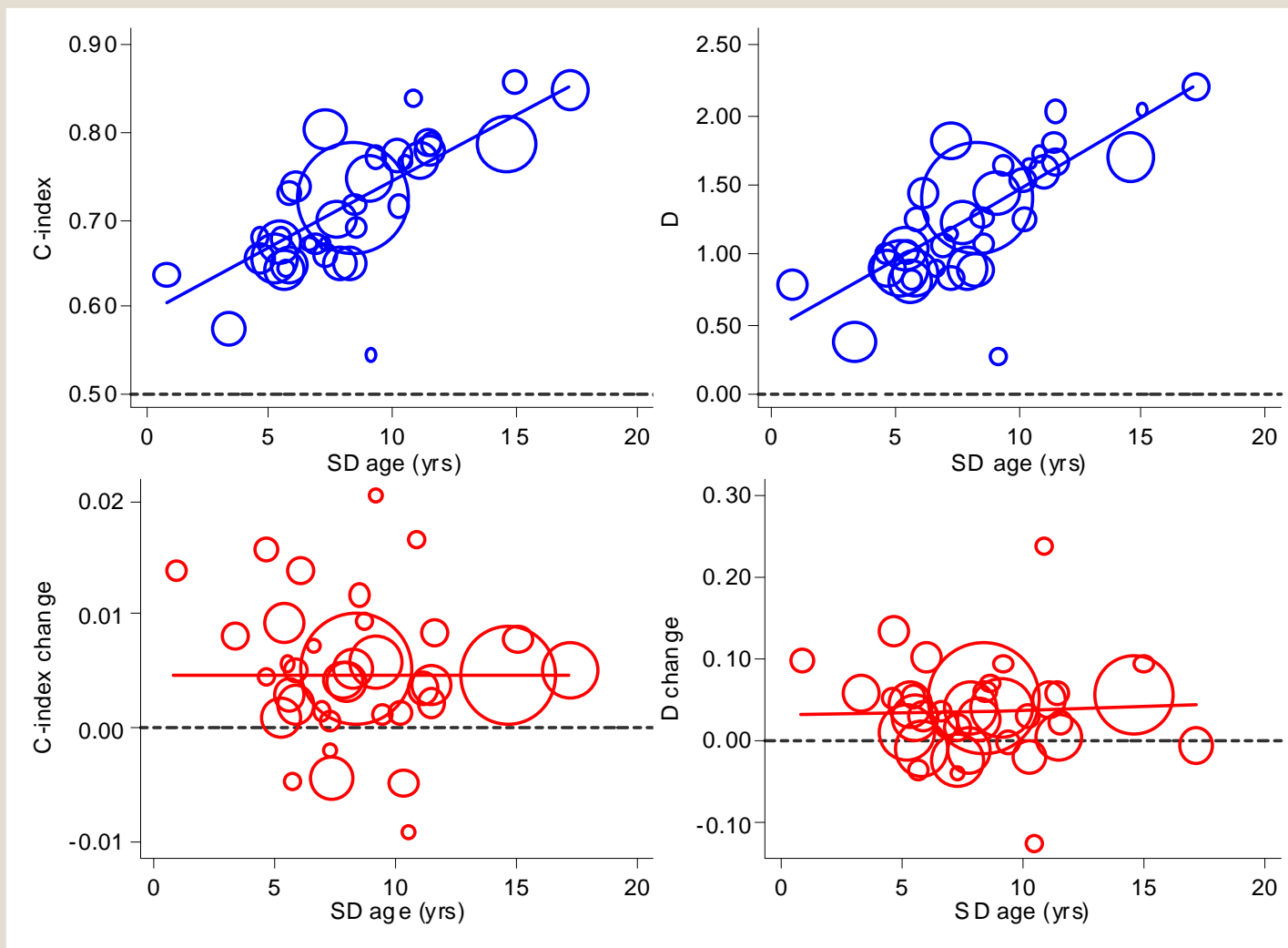


D change with addition of log CRP

Study-level relationship between C-index & D, ΔC & ΔD

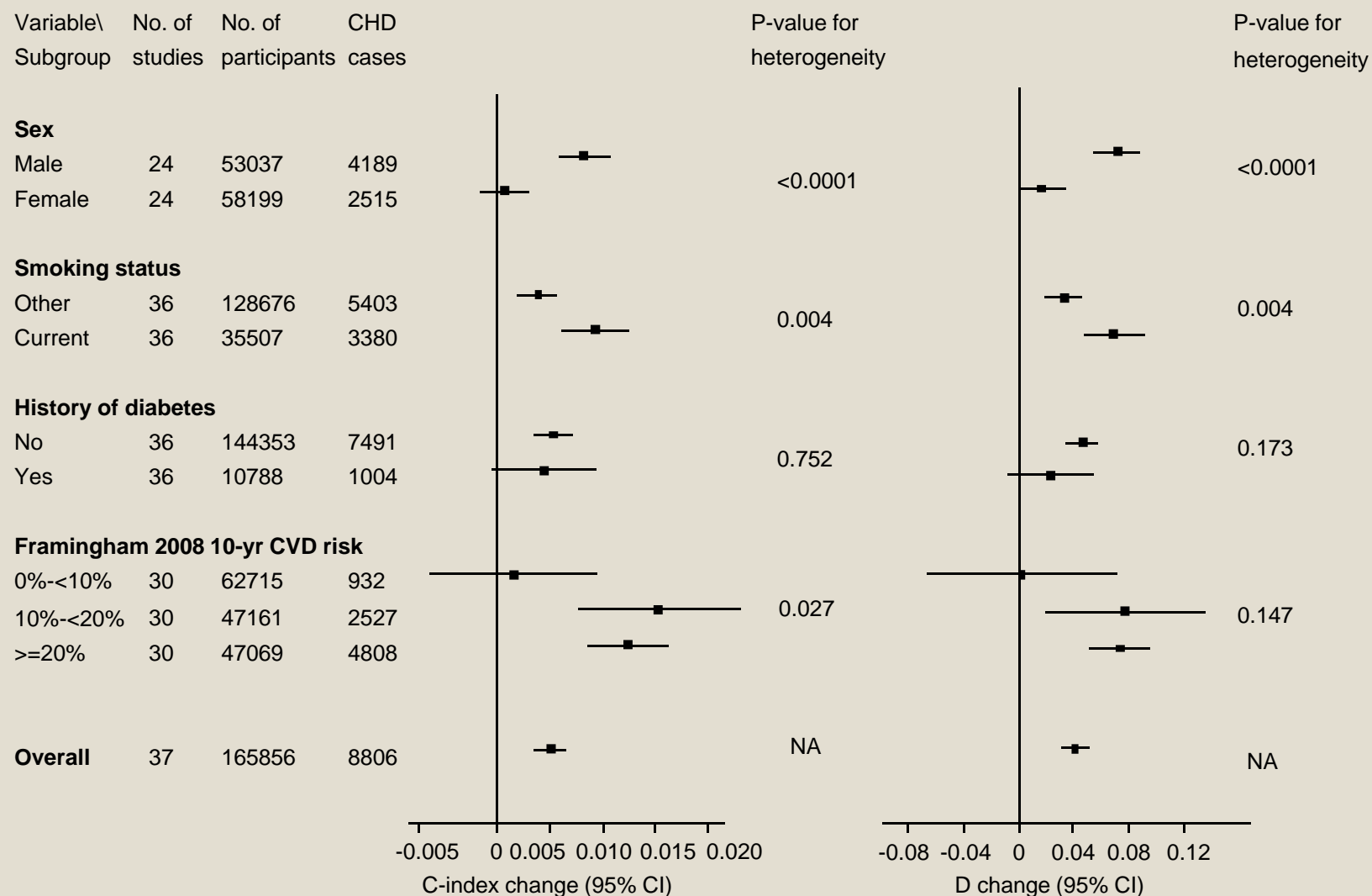


Between-study heterogeneity in absolute values of C-index or D is largely explained by age distribution



Size of circle is proportional to $1/\text{variance of estimate}$

Examination of subgroup effects – restricted to studies with all levels observed



Case-control studies are particularly problematic because of matching on predictive covariates

Study design \

Base model variables

Cohort (37 studies, 8806 CHD cases)

	C-statistic (95% CI)	C-statistic change (95% CI)	Z	P-value
Age	0.6441 (0.6383, 0.6499)	0.0224 (0.0191, 0.0258)	13.2	<0.0001
Above + smoking status	0.6614 (0.6558, 0.6671)	0.0153 (0.0126, 0.0180)	11.1	<0.0001
Above + systolic BP	0.6789 (0.6733, 0.6844)	0.0103 (0.0081, 0.0124)	9.2	<0.0001
Above + history of diabetes	0.6863 (0.6807, 0.6918)	0.0087 (0.0067, 0.0107)	8.5	<0.0001
Above + total cholesterol	0.6977 (0.6923, 0.7030)	0.0083 (0.0063, 0.0102)	8.4	<0.0001
Above + HDL cholesterol	0.7080 (0.7027, 0.7133)	0.0051 (0.0035, 0.0066)	6.3	<0.0001

Case-control (8 studies, 1566 CHD cases)

Age	0.4997 (0.4823, 0.5171)	0.0458 (0.0358, 0.0557)	9.0	<0.0001
Above + smoking status	0.5176 (0.5004, 0.5347)	0.0337 (0.0257, 0.0417)	8.2	<0.0001
Above + systolic BP	0.5430 (0.5261, 0.5600)	0.0246 (0.0178, 0.0313)	7.1	<0.0001
Above + history of diabetes	0.5506 (0.5337, 0.5676)	0.0224 (0.0160, 0.0289)	6.8	<0.0001
Above + total cholesterol	0.5849 (0.5681, 0.6017)	0.0191 (0.0130, 0.0252)	6.1	<0.0001
Above + HDL cholesterol	0.6053 (0.5888, 0.6218)	0.0122 (0.0070, 0.0173)	4.6	<0.0001

0.5 0.6 0.7 0.8

C-statistic (95% CI)

0 0.02 0.04 0.06

C-statistic change (95% CI), upon addition of log CRP

Stata software for IPD meta-analysis

<http://www.phpc.cam.ac.uk/ceu/research/erfc/stata/>

