



Non-parametric prediction and mapping of standing timber volume and biomass in a temperate forest

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Hooman Latifi¹, Arne Nothdurft², Barbara Koch¹

 ¹Dept. Of Remote sensing and Landscape information systems, University of Freiburg
 ²Dept. of Biometry and Informatics, Forest Research Institute Baden- Württemberg





Overview

∜Goal:

- Spatial predictions of Forest Variables, standing timber volume and biomass by non-parametric regression models
- Testing of various distance measures
- Variable selection

✤Data:

- Forest Inventory data (design attributes)
- Remote sensing data (predictor variables)
- Methods: Non-parametric regression models
 Results:
 - Performance (Bias, RMSE)
 - Variable Selection





Data Forest Inventory

Data from a forest inventory were collected on permanent circular sample plots in summer 2006

> 100×200 m sample grid

➤ The tree timber volume was calculated using the taper functions of Kublin (2003)

➤ Tree biomass with Zell's (2008) parameters for the allometric equation

> $B = \beta_0 d^{\beta_1} h^{\beta_2} + \epsilon$ d: diameter in breast height h: tree height $\beta_0, \beta_1, \beta_2$: tree specific function parameters

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Data Forest Inventory

Original 386 forest inventory sample plots
 297 complete reference sample plots were used
 means from the two data sets were not significantly different (t-test)
 prediction at plot-scale







Data Remote Sensing

The multispectral data

Useful for the delineation of vegetation covers

The active remote sensing data (e.g. LiDAR altimetry)

For characterization of highly variable forest canopy structures

(Koukoulas & Blackburg, 2005,IEEE Trans. Geo. Rem. Sens; Hudak et al., 2008,RSE).



Data Remote Sensing



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Data Remote Sensing

Optical data

- CIR orthoimages
- Thematic Mapper imagery

 <u>small footprint LiDAR data</u> (first-and-last pulses)
 Height
 intensity



Data



Remote sensing data LiDAR (light detection and range)

Visualized first-pulse LiDAR point cloud at a sample plot level





Telis

Non-parametric regression

the non-parametric k-nearest neighbor estimator

$$\hat{y}_k(x) = \frac{1}{n} \sum_{i=1}^n \omega_{ki}(x) y_i$$
 with weights $\omega_{ki}(x) = \begin{cases} n/k & \text{if } i \in J_x, \\ 0 & \text{otherwise.} \end{cases}$

denoted as Nadaraya-Watson-estimator:

$$\hat{y}_k(x) = \frac{\sum_{i=1}^n K_{d^{(k)}(x)}(d_i)y_i}{\sum_{i=1}^n K_{d^{(k)}(x)}(d_i)}$$

with uniform kernel estimator of variable bandwidth

$$K_{d^{(k)}}(u) = 1/2I\left(|u| \le d^{(k)}\right)$$

and distance between the vector of *p* variables for the target unit and its *k*-th neighbor

$$d^{(k)} = d^{(k)}(x)_{\text{s}}$$



Non-parametric regression

distance measure

$$d_i = \sqrt{(x - x_i)^T \Omega \left(x - x_i \right)}$$

Euclidian distance

Mahalanobis distance $\Omega = (Cov [X])^{-1}$

$$\Omega = diag\left\{p\right\}$$





Non-parametric regression

distance measure

$$d_i = \sqrt{\left(x - x_i\right)^T \Omega \left(x - x_i\right)}$$

Г

most similar neighbor MSN distance

$$\Omega = \Gamma \qquad \Lambda^2 \qquad \Gamma^T$$
$$p \times p \qquad p \times s \qquad s \times s \qquad s \times p$$

canonical coefficients

 $s = \min\left(p, t\right)$

canonical correlation coefficients Λ

Y

 $(n \times t)$

X

 $(n \times p)$

response variables

regressor variables

$$u_1 = X\alpha_1 , \quad v_1 = Y\beta_1$$
$$\vdots \quad , \qquad \vdots$$
$$u_s = X\alpha_s , \quad v_s = Y\beta_s$$





Non-parametric regression trees, Random Forests

In Random Forests (Breiman, 2001), the NNs are obtained by numerous solutions (forests) of classification trees.

The distance is calculated as one minus the proportion of terminal nodes from all regression trees where the target observation is in the same terminal node as the specific reference unit



Methods Variable selection



-The genetic algorithm (GA) applied for variable reduction is a search method that is based on the principle of evolution by natural selection.

[image removed]

(Trevino & Falciani, 2006)



Results *I- variable selection*

- GA search:
 - 11 variables for timber volume (7 from LiDAR
 21 predictors for biomass (15 from LiDAR)
 - mostly from FR height data

- Stepwise selection:
 - 5 predictors for timber volume (4 from LiDAR)
 4 predictors for biomass (3 from LiDAR)
 All from FR height data



Results



I- variable selection











comparison of RMSE for total timber volume

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method



comparing methods based on data sources-Biomass





comparison of RMSE for total Biomass



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Results



III- spatial predictions over the whole area (gridding)

Predictions of timber volume (left) and total biomass (right) by

- -RF method
- smoothed by An Epanechnikov-kernel with 100 m bandwidth







Discussion and Conclusion

Variable selection based on GA search was superior to stepwise selections

➢GA-selected variables (stabilized by a high solution rate) led to higher precision when applying Euclidean and Mahalanobis distances.

MSN and Random Forests worked better with the full regressor variable set

LiDAR-data were of major relevance



Disc

Discussion and Conclusion

➢All the applied methods yielded approximately unbiased predictions (Bias% <2%)</p>

Some of the forest stands have a dense understory, mainly composed of deciduous species, which may be a potential source of error in height metrics estimation

≻Further research:

Could the height metrics extracted from rasterized LiDAR forms improve the results?!





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Hooman Latifi