



Improving probabilities of correct decision in population enrichment designs

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End of Phase II

Biomarker suggests treatment is more effective in a subpopulation

- Biological plausibility
 - Biomarker is related to the mode of action of the experimental treatment
 - External data supporting the assumption about the potential predictive effect
- Subpopulation unambiguously defined
- Biomarker test kit is available and result is reliable





Motivating example – Phase II result

Primary end point of randomized phase II trial: PFS

- HR = 0.71 based on 110 events
 - HR \leq 0.75 is considered as relevant effect





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 - HR \leq 0.75 is considered as relevant effect
- Biomarker divide population into Subpopulation and Complement
 - HRs = 0.60 based on 50 events
 - HRc = 0.89 based on 50 events





Motivating example – Phase II result

Primary end point of randomized phase II trial: PFS

- HR = 0.71 based on 110 events
 - HR \leq 0.75 is considered as relevant effect
- Biomarker divide population into Subpopulation and Complement
 - HRs = 0.60 based on 50 events
 - HRc = 0.89 based on 50 events
- Plan phase III trial with one interim analysis for potential subpopulation selection





Phase III Setting

- θ is overall treatment effect, i.e. -log(HR)
 - θ >0 ⇔ HR<1</p>
- Hypothesis tested in Sub and Full population
 - Hs: θs≤ 0 against θs > 0
 - H_F: θ≤ 0 against θ > 0





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 - − H_F: θ ≤ 0 against θ > 0
- Relationship between θ and θ s
 - $\theta = \gamma \theta s + (1-\gamma) \theta c$
 - $-\gamma$ is subpopulation fraction





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 - Hs: θs≤ 0 against θs > 0
 - − H_F: θ ≤ 0 against θ > 0
- Relationship between θ and θ s
 - $\theta = \gamma \theta s + (1-\gamma) \theta c$
 - $-\gamma$ is subpopulation fraction
- 508 events correspond to 90% Power with one-sided α=0.025 and planned HR=0.75
- One interim analysis is performed after τ% of subjects/events are collected
 - $-\tau$ is information fraction





Closed testing procedure







Stage 1

Stage 2

- Options after Stage 1
 - Continue with the full population
 - Continue with the sub population
 - Stop for futility
 - Stop for efficacy: no option





Combine data from stage 1 and 2

Inverse normal method

$$C(p_{1,J}, p_{2,J}) = w_1 \Phi^{-1}(1 - p_{1,J}) + w_2 \Phi^{-1}(1 - p_{2,J})$$

- with $J \subseteq \{F, S\}$
- Weights: $w_1 = \sqrt{\tau} \quad w_2 = \sqrt{1 \tau} \quad (w_1^2 + w_2^2 = 1)$





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- with J<u></u>{F,S}
- Weights: $w_1 = \sqrt{\tau} \quad w_2 = \sqrt{1 \tau} \quad (w_1^2 + w_2^2 = 1)$
- Intersection hypothesis: Hochberg procedure
- Second stage p-values based on increments in survival setting



Continue with the full population Stage 1 Stage 2 P1,FS P2,FS P1,F P2,F P1,F P2,F

Reject H_F in stage 2, if min(C(p1,FS, p2,FS), C(p1,F, p2,F))> $\Phi^{-1}(1-\alpha)$

Reject Hs in stage 2, if min(C(p1,FS, p2,FS), C(p1,S, p2,S))> $\Phi^{-1}(1-\alpha)$



Continue with the sub population Stage 1 Stage 2 P1,FS P2,S P2,S P1,F P1,S P2,S

Reject Hs in stage 2, if min(C(p1,FS, p2,S), C(p1,S, p2,S))> $\Phi^{-1}(1-\alpha)$



Stop for futility

Stage 1





How to make an interim decision?





- How to make an interim decision?
- How to make the correct interim decision?





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- How to make the correct interim decision?
 - Let's say HR≤0.75 is considered as clinically relevant
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 - Let's say HR≤0.75 is considered as clinically relevant
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 - What would be the decision if (subpopulation fraction γ=0.5)
 - HR_F =0.75, HR_s =0.75, HR_c =0.75 ?





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- How to make the correct interim decision?
 - Let's say HR≤0.75 is considered as clinically relevant
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 - What would be the decision if (subpopulation fraction γ=0.5)
 - HR_F=0.75, HR_s=0.75, HR_c=0.75?
 - HR_F=0.75, HR_S=0.74, HR_c=0.76 ?





- How to make an interim decision?
- How to make the correct interim decision?
 - Let's say HR≤0.75 is considered as clinically relevant
 - Let's say we know the truth
 - What would be the decision if (subpopulation fraction γ=0.5)
 - HR_F=0.75, HR_s=0.75, HR_c=0.75?
 - HR_F=0.75, HR_s=0.74, HR_c=0.76?
 - HR_F =0.75, HR_s =0.70, HR_c =0.81 ?
 - HR_F=0.77, HR_s=0.70, HR_c=0.85 ?





- How to make an interim decision?
- How to make the correct interim decision?
 - Let's say HR≤0.75 is considered as clinically relevant
 - Let's say we know the truth
 - What would be the decision if (subpopulation fraction γ=0.5)
 - HR_F=0.75, HR_s=0.75, HR_c=0.75?
 - HR_F=0.75, HR_S=0.74, HR_c=0.76?
 - HRF=0.75, HRs=0.70, HRc=0.81 ?
 - HR_F=0.77, HR_s=0.70, HR_c=0.85 ?
 - Let's focus on the unambiguous scenarios
 - $HR_F = 0.75$, $HR_S = 0.75$, $HR_C = 0.75 \Rightarrow$ go with the full population
 - $HR_F = 0.87$, $HR_S = 0.75$, $HR_C = 1 \implies$ go with the sub population
 - $HR_F = ?$, $HR_S = 1$, $HR_C = ? \Rightarrow$ stop for futility



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 - Maximally one of these scenarios can be true
 - Make assumption how likely the different scenarios are



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 - Maximally one of these scenarios can be true
 - Make assumption how likely the different scenarios are
 - Q = P(correct decision in interim analysis)
 - = $\sum P(\text{correct decision} | \text{true values in sub } \cap \text{ in complement}) * P(\text{true values in sub } \cap \text{ in complement})$



Main focus of this talk

- How to make an interim decision?
- How to make the correct interim decision?
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 - $HR_F = 0.75$, $HR_S = 0.75$, $HR_C = 0.75 \Rightarrow$ go with the full population
 - $HR_F = 0.87$, $HR_S = 0.75$, $HR_C = 1 \implies$ go with the sub population
 - $HR_F = ?$, $HR_S = 1$, $HR_C = ? \Rightarrow$ stop for futility
 - Maximally one of these scenarios can be true
 - Make assumption how likely the different scenarios are
 - Q = P(correct decision in interim analysis)

= $\sum P(\text{correct decision} | \text{true values in sub} \cap \text{ in complement}) * P(\text{true values in sub} \cap \text{ in complement})$

- $=\omega_1$ P(continue full | effect in sub \cap effect in complement)
- + ω_2 P(continue sub | effect in sub \cap no effect in complement)
- $+\omega_3$ P(stop for futility | no effect in sub),

 $(\omega_1 + \omega_2 + \omega_3 = 1)$





How to make the interim decision?

Sign of the observed treatment effect ("Simple rule")

- $\hat{\theta}_{s} < 0$:
- $\hat{\theta}_{s} >= 0 \& \hat{\theta}_{c} < 0$:
- $\hat{\theta}_{s} >= 0 \& \hat{\theta}_{c} >= 0:$

- Stop for futility
- Continue sub
- Continue full







How to make the interim decision?

Sign of the observed treatment effect ("Simple rule")

- $\hat{\theta}_{s} < 0$: Sto
- $\hat{\theta}_{s} >= 0 \& \hat{\theta}_{c} < 0$:
- $\hat{\theta}_s \ge 0 \& \hat{\theta}_c \ge 0$:



Continue full



General "linear rule"

- $\hat{\theta}_{s} < f_{L}$: Stop for futility • $\hat{\theta}_{s} >= f_{L} \& a_{L} * \hat{\theta}_{s} + \hat{\theta}_{c} < d_{L}$: Continue sub
- $\hat{\theta}_s \ge f_L \& a_L * \hat{\theta}_s + \hat{\theta}_c \ge d_L$: Continue full







Find optimal decision rule

- Q_L = P(correct decision in interim analysis)
 - $= \omega_1 P(X > f_L, Y > d_L | E(X) = -\log(0.75), E(Y) = a_L^*(-\log(0.75)) + (-\log(0.75)))$

+ $\omega_2 P(X > f_L, Y < d_L | E(X) = -log(0.75), E(Y) = a_L^*(-log(0.75)) + (-log(1)))$

+ $\omega_3 P(X < f_L | E(X) = -log(1))$

- Find optimal values (max(Q_L)) for boundaries
 - a∟, d∟, f∟





- Assumption about true effects
 - (θs, θc) =(0,)
 - $(\theta s, \theta c) = (\log(1/0.75), 0)$
 - $(\theta s, \theta c) = (\log(1/0.75), \log(1/0.75))$ continue full

stop for futility continue sub continue full





- Assumption about true effects
 - $(\theta s, \theta c) = (0,)$
 - (θ s, θ c)=(log(1/0.75),0)
 - $(\theta s, \theta c) = (\log(1/0.75), \log(1/0.75))$ continue full
- Subpopulation fraction γ
- Information fraction τ

stop for futility continue sub



- Assumption about true effects
 - $(\theta s, \theta c) = (0,)$
 - (θ s, θ c)=(log(1/0.75),0)
 - $(\theta s, \theta c) = (\log(1/0.75), \log(1/0.75))$ continue full
- Subpopulation fraction γ
- Information fraction τ
- Timing of final analysis
 - Continue full population:
 - 508 events in full population, ~ γ *508 events in sub population _

- stop for futility
- continue sub



- Assumption about true effects
 - $(\theta s, \theta c) = (0,)$
 - (θ s, θ c)=(log(1/0.75),0)
 - $(\theta s, \theta c) = (\log(1/0.75), \log(1/0.75))$ continue full
- Subpopulation fraction γ
- Information fraction τ
- Timing of final analysis
 - Continue full population:
 - 508 events in full population, ~ γ *508 events in sub population
 - Continue sub population
 - 508 events in sub population

- stop for futility
- continue sub

Determine "optimal" boundaries

- Assumption about true effects
 - (θs, θc) =(0,)
 - (θ s, θ c)=(log(1/0.75),0)
 - $(\theta s, \theta c) = (\log(1/0.75), \log(1/0.75))$ continue full
- Subpopulation fraction γ
- Information fraction τ
- Timing of final analysis
 - Continue full population:
 - 508 events in full population, ~ γ *508 events in sub population
 - Power 90%, ...
 - Continue sub population
 - 508 events in sub population
- Weights (ω_1 , ω_2 , ω_3) depending on prior assumption
 - (full, sub, stop)
 - (1/3, 1/3, 1/3)
 - (0.4, 0.4, 0.2)

stop for futility continue sub continue full







"Optimal" boundaries for linear rule

- $\hat{\theta}_{s} < f_{L}$: Stop for futility
- $\bullet \quad \hat{\theta}_{_{S}} \! > \! = f_L \And a_L \! \ast \, \hat{\theta}_{_{S}} \, + \hat{\theta}_{_{C}} < \, d_L \! : \ \ Continue \ sub$
- $\hat{\theta}_s \ge f_L \& a_L * \hat{\theta}_s + \hat{\theta}_c \ge d_L$: Continue full
- a_{\perp} often $0 \Rightarrow$ decision between sub and full based on complement
- Usually dL > fL





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- $\hat{\theta}_s \ge f_L \& a_L * \hat{\theta}_s + \hat{\theta}_c \ge d_L$: Continue full
- a_{\perp} often $0 \Rightarrow$ decision between sub and full based on complement
- Usually dL > fL
- Example for subpop=0.5, information=0.3, weights (full, sub, stop)=(1/3, 1/3, 1/3)
 - HRs > 0.95
 Stop for futility
 - HRs ≤ 0.95 & HRc > 0.86 Continue sub
 - $HRs \le 0.95$ & $HRc \le 0.86$ Continue full





"Optimal" boundaries for linear rule

- $\hat{\theta}_{s} < f_{L}$: Stop for futility
- $\hat{\theta}_s \ge f_L \& a_L * \hat{\theta}_s + \hat{\theta}_c < d_L$: Continue sub
- $\hat{\theta}_s \ge f_L \& a_L * \hat{\theta}_s + \hat{\theta}_c \ge d_L$: Continue full
- a_{\perp} often $0 \Rightarrow$ decision between sub and full based on complement
- Usually dL > fL
- Example for subpop=0.5, information=0.3, weights (full, sub, stop)=(1/3, 1/3, 1/3)
 - HRs > 0.95
 Stop for futility
 - HRs ≤ 0.95 & HRc > 0.86 Continue sub
 - HRs ≤ 0.95 & HRc ≤ 0.86 Continue full
- Example for subpop=0.5, information=0.3, weights (full, sub, stop)=(0.4, 0.4, 0.2)

Stop for futility

- HRs > 1.05
- HRs ≤ 1.05 & HRc > 0.86 Continue sub
- $HRs \le 1.05$ & $HRc \le 0.86$ Continue full

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Performance comparison - Simulation

- Simulation of normalized test statistics based on all pairwise combinations of (0.65, 0.75, 0.85, 1) for $(1/\exp(\theta s), 1/\exp(\theta c))$
- Optimal boundaries for
 - $(\theta s, \theta c) = (0,)$
 - $(\theta s, \theta c) = (-\log(0.75), 0)$
 - (θ s, θ c)= (-log(0.75), -log(0.75)) continue full
- Results
 - Rate of correct interim decision
 - Power (reject at least one)

stop for futility

- continue sub



Probabilities of Interim Decisions (%)

Optimal Linear rule		(1/3,1/3,1/3)			(0.4,0.4,0.2)			
HR_S	HR_C	HR_F	full	sub	futility	full	sub	futility
0.650	1.000	0.806	24.8	70.1	5.1	25.9	72.3	1.8
0.750	0.750	0.750	60.9	23.9	15.2	66.5	26.2	7.2
0.750	1.000	0.866	21.6	63.4	15.0	23.3	70.0	6.7
1.000	1.000	1.000	11.1	30.2	58.7	15.8	42.6	41.6



Probabilities of Interim Decisions (%)

Optimal L	inear rule		(1	/3,1/3,1	/3)	(0.4,0.4,0.2)		
HR_S	HR_C	HR_F	full	sub	futility	full	sub	futility
0.650	1.000	0.806	24.8	70.1	5.1	25.9	72.3	1.8
0.750	0.750	0.750	60.9	23.9	15.2	66.5	26.2	7.2
0.750	1.000	0.866	21.6	63.4	15.0	23.3	70.0	6.7
1.000	1.000	1.000	11.1	30.2	58.7	15.8	42.6	41.6
Simple ru	le							
HR_S	HR_C	HR_F	full	sub	futility			
0.650	1.000	0.806	48.7	48.3	3.0			
0.750	0.750	0.750	79.8	9.6	10.6			
0.750	1.000	0.866	45.6	44.1	10.3			
1.000	1.000	1.000	25.3	24.7	50.1			



P(Reject at least one) (%)

			Optimal Lin	ear rule	Simple rule	Ctp w/o IA
HR_S	HR_C	HR_F	(1/3,1/3,1/3)	(0.4,0.4,0.2)		
0.650	1.000	0.806	93.1	96.2	93.1	90.7
0.750	0.750	0.750	76.7	82.8	78.8	86.2
0.750	1.000	0.866	72.7	78.0	67.6	56.5
1.000	1.000	1.000	1.7	1.8	1.6	2.2





Discussion

- Evaluation of decision rules in planning phase is important
 - Optimizing decision rules can substantially improve probabilities of correct decision and power compared to "intuitive" decision rules
- Assumption or prior knowledge needed
 - Strong impact on results
 - Recommendation with promising results from phase II: not too much weight on stopping for futility
- Extension to other type of decision rule easy
 - For example: conditional power (CP)
 - CP_s < f_{CP}: Stop for futility
 - $\label{eq:cps} \bullet \quad CP_s \mathrel{>=} f_{CP} \ \& \ CP_s \mathrel{>=} \ CP_F \mathrel{+} d_{CP}: \quad Continue \ sub$
 - $CP_s \ge f_{CP} \& CP_s < CP_F + d_{CP}$: Continue full

- "Optimal" CP rule lead to similar decisions as "optimal" linear rule





So far...

- "Points/lines" determine correct decisions
- Weights define how likely each case is (e.g. (full, sub, stop)=(0.4, 0.4, 0.2))







Extension

- "Areas" determine correct decisions
- Prior distribution based on phase II data define how likely each case is



$$f_{u_s}$$
: N(-log(0.6), 4/50), f_{u_c} : N(-log(0.89), 4/50)



References

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Back up

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"Optimal" boundaries for linear rule

 ω_2

γ

 ω_1

τ

exp(0.15) = 1.16
exp(0.10) =1.11
exp(0.05) =1.05
exp(-0.05)=0.95
exp(-0.10)=0.90
exp(-0.20)=0.82

		0.05	0.15	0.00	1/3	1/3	1/3	0.375	0.3	_1 16
		-0.15	0.15	0.00	0.2	0.4	0.4	0.375	0.3	=1.10 =1.11 =1.05
		-0.20	0.10	0.00	0.15	0.35	0.5	0.375	0.3)=0.95)=0.90
		-1.00*	0.15	0.00	0	0.5	0.5	0.375	0.3)=0.82
		0.05	0.15	0.00	1/3	1/3	1/3	0.5	0.3	
		-0.05	0.15	0.00	0.2	0.4	0.4	0.5	0.3	
		-0.10	0.05	-0.10	0.15	0.35	0.5	0.5	0.3	
		-1.00*	0.15	0.00	0	0.5	0.5	0.5	0.3	
		0.10	0.15	0.00	1/3	1/3	1/3	0.375	0.6	
		0.00	0.15	0.00	0.2	0.4	0.4	0.375	0.6	
		-0.05	0.10	-0.05	0.15	0.35	0.5	0.375	0.6	
		-1.00*	0.15	0.00	0	0.5	0.5	0.375	0.6	
	ô C	0.10	0.10	-0.10	1/3	1/3	1/3	0.5	0.6	
Stop for futili	$\theta_{s} < t_{L}$:	0.05	0.15	0.00	0.2	0.4	0.4	0.5	0.6	
$a_L * \theta_s + \theta_c < d_L$: Continue	$\theta_s >= f_L \& a_L$	0.00	0.10	-0.05	0.15	0.35	0.5	0.5	0.6	
$a_{L} * \hat{\theta}_{s} + \hat{\theta}_{c} >= d_{L}$: Continue d	$\hat{\theta}_s \ge f_L \& a_L $	-1.00*	²⁰ 10.15	ns 25 June 0.00	nment desig	lation enricl	sion in popu	correct deci	babilities of 0.6	Improving pro

 f_{L}

 d_L

 a_L

 ω_3



Phase II results often not conclusive





Simulated Study - 12 months recruit 8 months follow up



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