



# Improved species distribution models with explicit modelling of spatial autocorrelation: challenges and perspectives using INLA and SPDE

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- Spatial effects in SDMs
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# Species distribution models and tree species suitability

- Tree species adapted to future climate conditions?

- Practical: Field trials

- Modelling: landscape models, vegetation models, single-tree growth models, etc. ... Species Distribution Models (SDMs)

How good are SDMs in reflecting the ecophysiological potential of a tree species (fundamental niche)?

- ... epigenetic effect and local adaptations?

- ... phenology?

- ... biotic interactions?

- ... competition and facilitation?

- Booth (2018), Garzón et al. (2019)

# Spatial effects in SDMs

- Tree species occurrence and associated climate- and soil data are not independent from another
- Spatial Autocorrelation (SAC) may bias model results

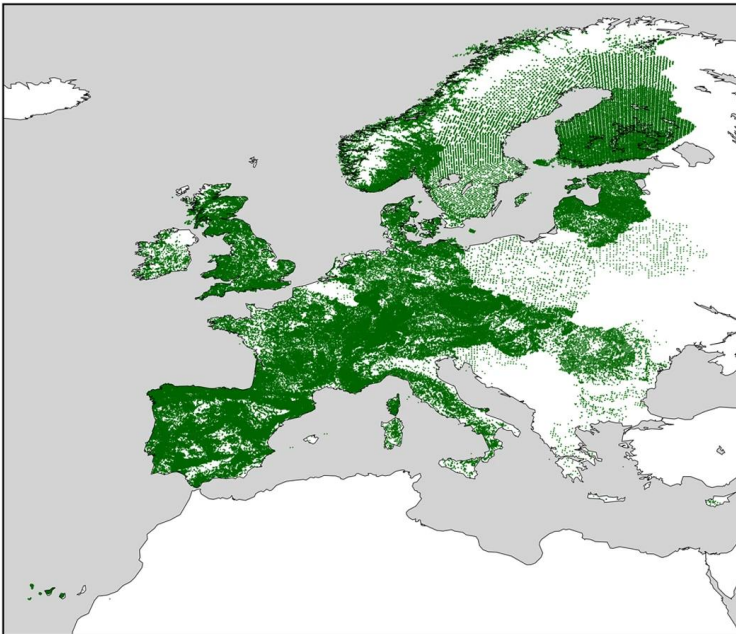


Fig. 1: Species distributions in Mauri et al. (2017)

Possible causes:

- Inventory design
  - Historical processes
  - Biotic processes
- etc.

Dealing with SAC?

- Remove SAC effects (Wavelet Revised Models (Carl & Kühn, 2010))
- Estimate residual spatial autocorrelation (Dormann et al., 2007)

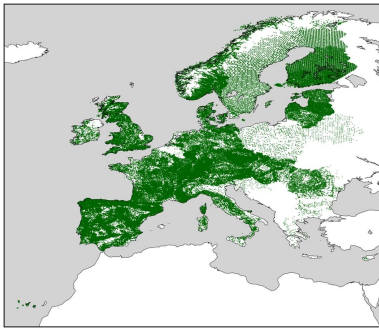
# Bayes-modelling approach with INLA and SPDE

- Estimating the spatial dependency of tree species occurrences with a covariance function
- Computational expensive: changing covariance into precision matrices
- Approximation of the covariance function with Stochastic Partial Differential Equations (SPDE) and the finite-element method (Lindgren et al. 2011)
- Model inference with Integrated Nested Laplace Approximation INLA, Rue et al. (2009)

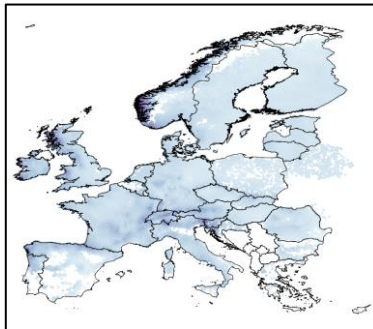
# Bayes-modelling approach with INLA and SPDE

- R software with package R-INLA (Rue et al. 2009) and mgcv (Wood 2017)
- Constructing a SPDE-smooth in GAMs possible (Miller et al. 2019)
- Matérn basis-penalty SPDE smoother with hyperparameters  $\kappa$  and  $\tau$

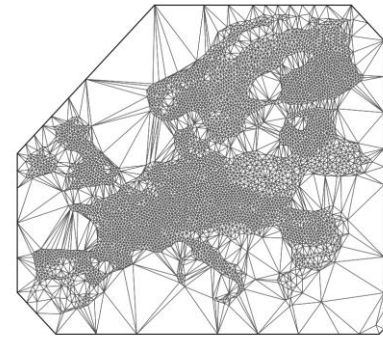
Species occurrences based on Mauri et al. (2017)



Bioclimatic variables based on Karger et al. (2017)



Use SPDE-smooth in GAM



- Binomial GAMs with logit-link, REML and INLA estimation (Wood 2019)
- Variable selection (Marra & Wood 2011), Concurvity reduction (Wood 2017)

# Model results

Species	AUC (without/with SPDE)		AIC (without/with SPDE)		TSS (without/with SPDE)	
<i>Picea abies</i> (L.) Karst.	0.87	0.91	154.533	133.100	0.61	0.67
<i>Abies alba</i> Mill.	0.89	0.94	51.451	42.478	0.63	0.75
<i>Pinus sylvestris</i> L.	0.79	0.86	196.928	168.672	0.41	0.54
<i>Fagus sylvatica</i> L.	0.83	0.89	138.772	115.724	0.49	0.59
<i>Quercus robur</i> L.	0.84	0.90	125.075	105.425	0.49	0.63



# Model results

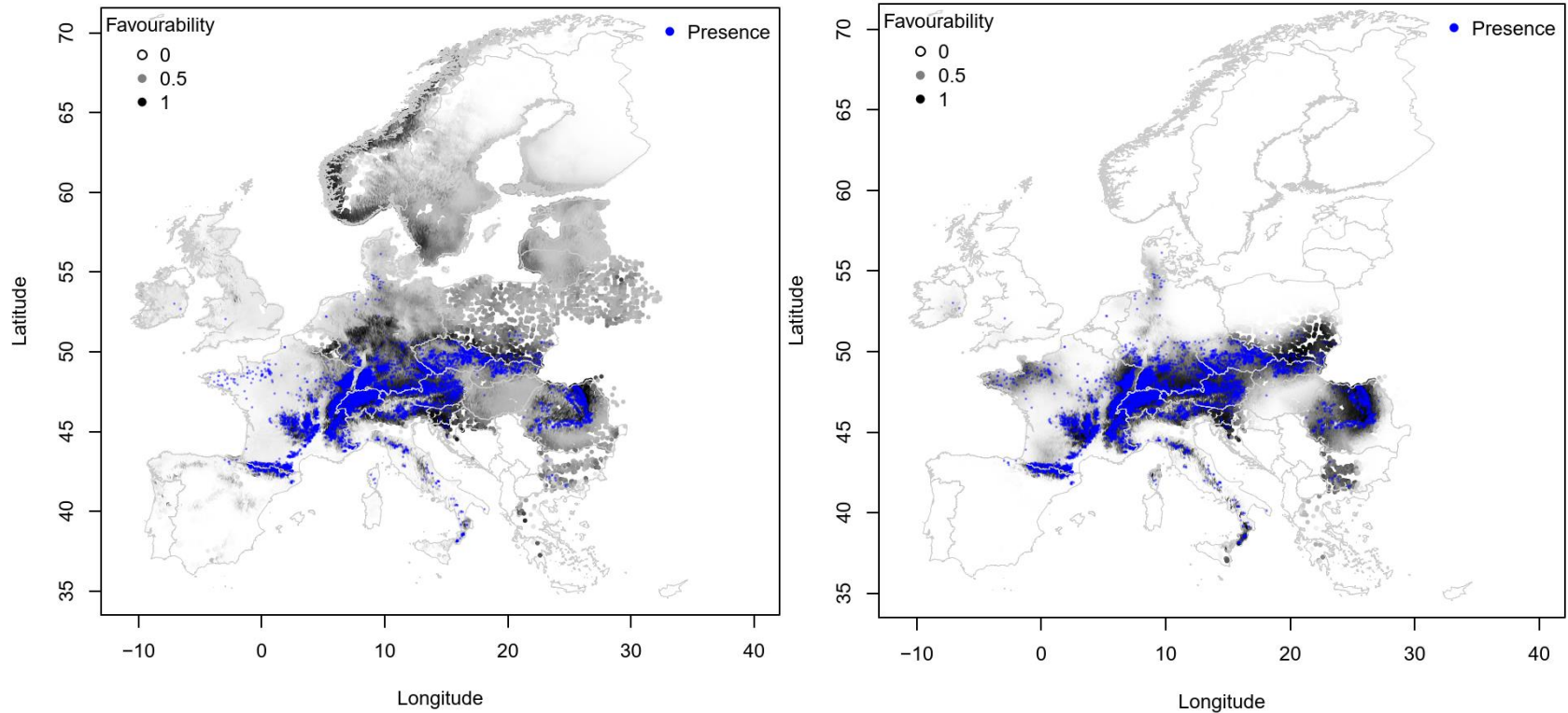


Fig. 2: Species favourability prediction for *Abies alba* Mill. Without (left) and with (right) SPDE-smooth in the model.



# Improved tree species suitability with conditional predictions?

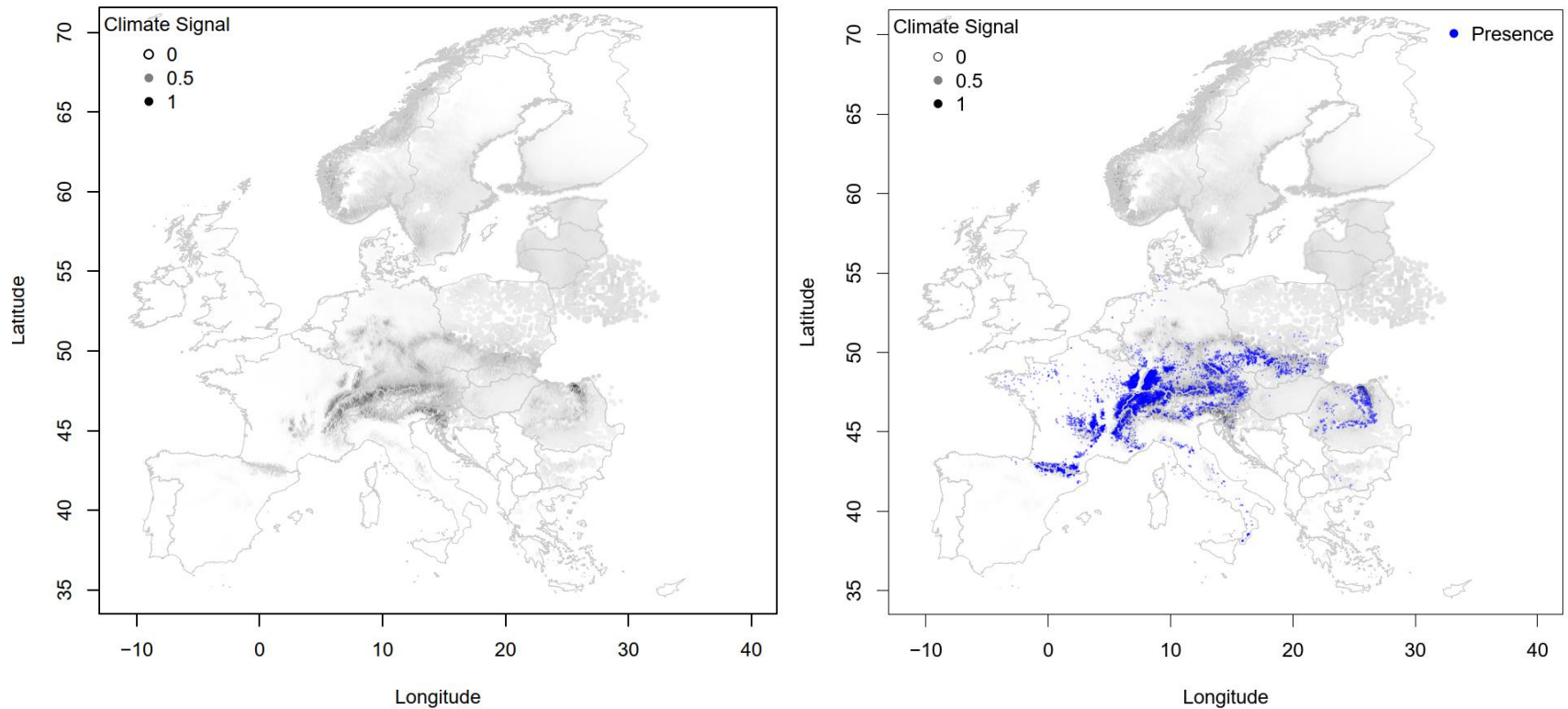


Fig. 3: Climate signal of the conditional predictions for *Abies alba* Mill.

# Summary

- INLA and SPDE enable computational effective estimation of spatial effects in SDMs
- Variable selection is still of high importance
- Harmonization of heterogenous data sets possible with INLA und SPDE
- Conditional predictions can remove spatial effects
- Improved identification of core and marginal ecological ranges of a species
- Better approximation fo the fundamental niche of a species

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