

**A relative survival model for clustered responses -  
Comparing SAS PROC NLMIXED and WinBUGS for  
parameter estimation**

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## Relative Survival I: Definition

For a group of patients:

$$\text{Relative Survival} = \frac{\text{Observed Survival}}{\text{Expected Survival}}$$

where expected survival is derived from published age-, sex-, and calendar time-specific mortality rates.

**Interpretation:** Relative Survival describes survival in a hypothetical population where the disease of interest is the only cause of death (and is therefore the standard method in disease registries).

## **Relative Survival II: Properties**

### **Advantages:**

- Information on cause of death is not needed.
- Cure (in a statistical sense) can be described.

### **Disadvantages:**

- Information on mortality of the general population is needed.
- Patients group must be a sample from the general population.

## Relative Survival III: Regression Models

Generalizing the pure description, regression models for relative survival have been proposed to describe influence of prognostic and risk factors (Hakulinen/Tenkanen, 1987; Estève et al., 1990)

Owing to the principle of relative survival these are all *additive* hazard models:

$$\lambda_{obs} = \lambda_{pop} + \lambda_{excess} \quad (1)$$

with  $\lambda_{obs}$  = observed hazard,  $\lambda_{pop}$  = population hazard,  $\lambda_{excess} = \exp(X\beta)$ : excess hazard, function of the covariates

Compare this to the Cox model:  $\lambda_{obs} = \lambda_0 \exp(X\beta)$  (*multiplicative* model)

## Relative Survival IV: The Estève model as a GLM I

Dickmann et al., 2004, showed that the Estève model can be written as a GLM with a binary response, a Poisson likelihood, an offset and a specific individualized link function.

**Notation:** Given are  $i = 1, \dots, N$  patients, each one observed for  $j = 1, \dots, J_i$  annual intervals.

$\delta_{ij}$  is the event indicator in the  $ij$ -th interval ( $\delta_{ij} = 1$  refers to dying,  $\delta_{ij} = 0$  to surviving).

$r_{ij}$  denotes the time at risk (in %), and  $e_{ij}^* = (\lambda_{pop} * r_{ij})$  the weighted population hazard in the  $ij$ -th interval.

## Relative Survival V: The Estève model as a GLM II

The model equation is

$$\ln(\mu_{ij} - e_{ij}^*) = \ln(r_{ij}) + x_i\beta. \quad (2)$$

There is no correlation induced by the  $J_i$  observations per pro-band!

Model assumes proportional hazard assumption for the covariates and constant hazard in annual intervals!

## **Motivation I: The HALLUCA study**

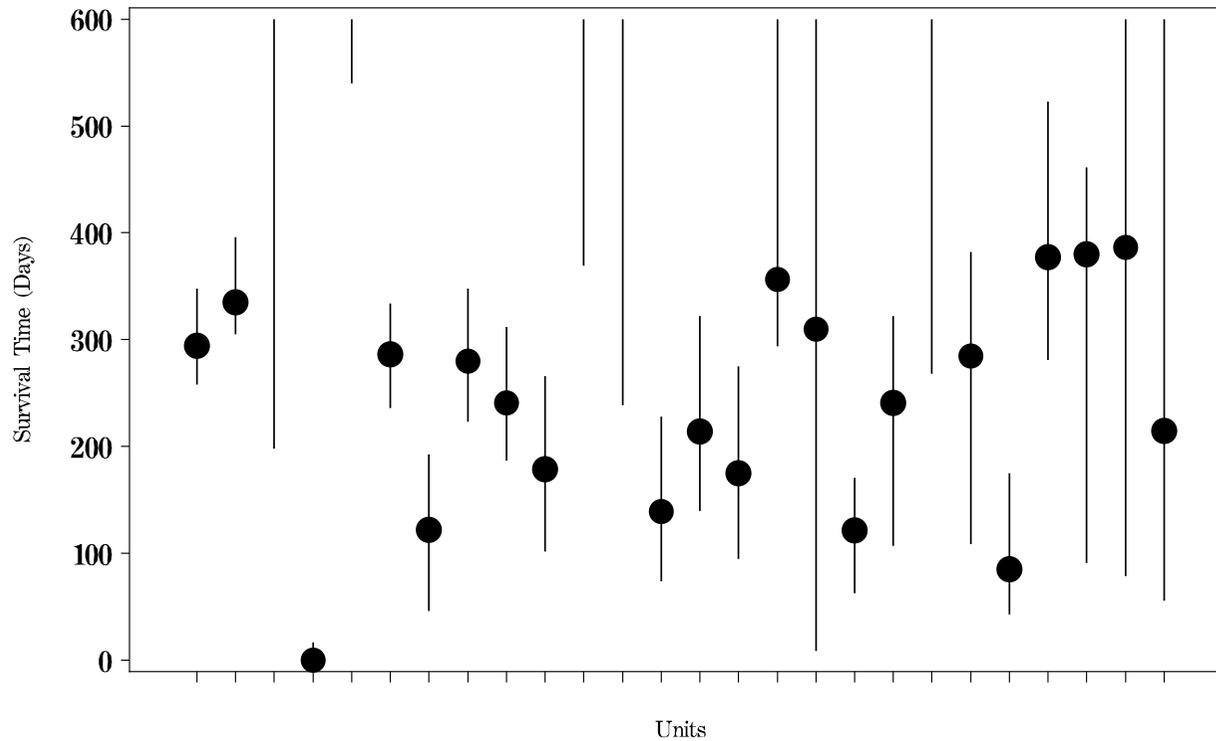
HALLUCA-(= Halle Lung Carcinoma)-study, an epidemiological study which investigated provision of medical care of lung cancer patients in the region of Halle.

Standardized recruiting of all lung cancer patients from 4/1996 to 9/1999, follow-up until 9/2000.

N=1696 lung cancer patients, 1349 patients (79.5%) died until the end of follow-up, median survival in the study population was 284 days (=9.3 months).

Data on population mortality was achieved from the Statistical Office of the State of Saxony-Anhalt ('Statistisches Landesamt Sachsen-Anhalt').

## Motivation II: Heterogeneous Survival in Diagnostic Units



Observed median survival (with 95% confidence intervals) in the 26 diagnostic units with more than 5 patients.

## A Relative Survival Model for Clustered Responses I

Generalize Dickman's model to account for clustered (or, equivalent, correlated within units) responses by adding a random effect for the diagnostic unit in the linear predictor, achieving a generalized linear mixed model (GLMM).

To be concrete,  $\delta_{hij}$  denotes the event indicator for individual  $i$  from cluster  $h$  ( $h = 1, \dots, H$ ), then

$$\ln(\mu_{hij} - e_{ij}^*) = \ln(r_{ij}) + x_i\beta + u_h \quad (3)$$

The random intercept  $u_h$  is assumed to be normally distributed with variance  $\sigma_h^2$ ,  $u_h \sim N(0, \sigma_h^2)$ .

## **A Relative Survival Model for Clustered Responses II**

Parameter estimation in this random effects relative survival models, as in all GLMM, is complicated by the fact that the likelihood function consists of  $H$  integrals which are not analytically tractable.

We used numerical (SAS PROC NLMIXED) and stochastic integration (WinBUGS) for parameter estimation.

Additional complication: individualized link functions

## Computation I: SAS PROC NLMIXED

```
proc nlmixed data=... ;  
  parms int=-1 b_stage2=0.5 b_stage3=0.7 ... sd2=1;  
  
  Xbeta = int + b_stage2*stage2 + b_stage3*stage3 + ... + u_h;  
  
  Mu      = exp(Xbeta+log_r_ij) + e_ij;  
  
  loglike = delta_ij*log(Mu) - Mu;  
  model delta_ij ~ general(loglike);  
  random u ~ normal(0,sd2_h) subject=DiagnosticUnit;  
run;
```

## Computation II: WinBUGS

```
model; {
  for (i in 1:N){
    Xbeta[i] <- int + b_stage2*stage2[i] + b_stage3*stage3[i] + ...
              + u_DiagnosticUnit[DiagnosticUnit[i]];

    log(mu[i]) <- log(r_ij[i]) + Xbeta[i]+ exp(e_ij[i]);
    delta_ij[i] ~ dpois(mu[i]);
  }
  for (h in 1:H){
    u_DiagnosticUnit[h]~ dnorm(0.0000, tau_DiagnosticUnit);
  }

  tau_DiagnosticUnit ~ dgamma(0.001,0.001);
  var_DiagnosticUnit <- 1 / tau_DiagnosticUnit;

  # priors
  int~ dnorm(0.0,1.0E-6) b_stage2~ dnorm(0.0,1.0E-6) ...
}
```

## Results I: Fixed effects (selected)

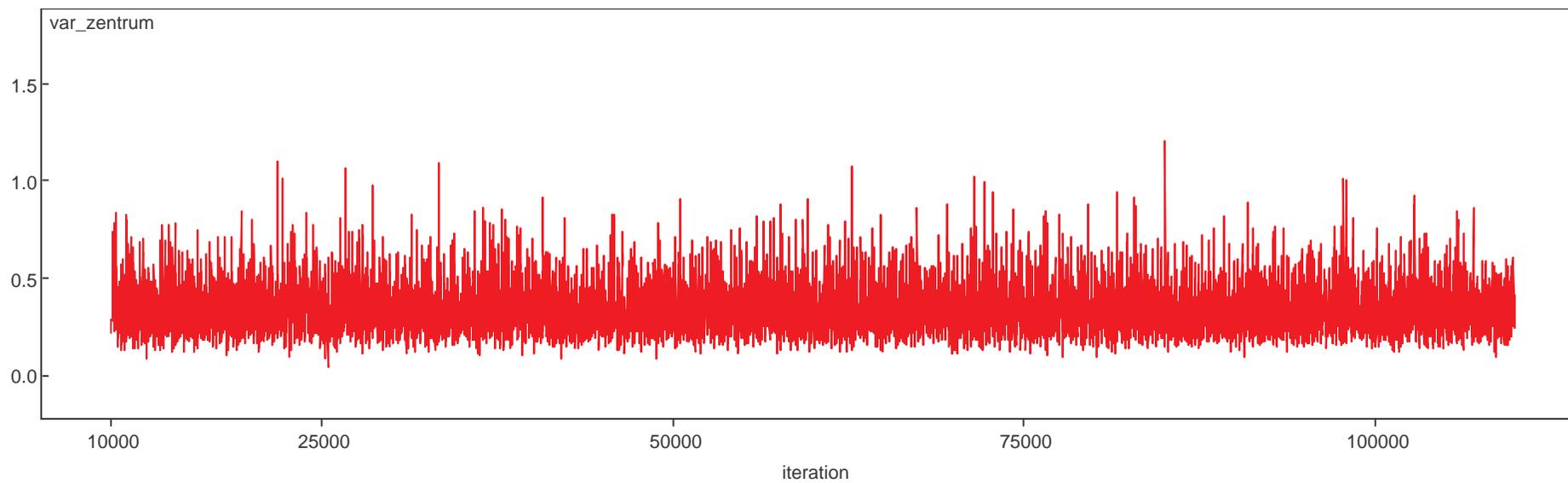
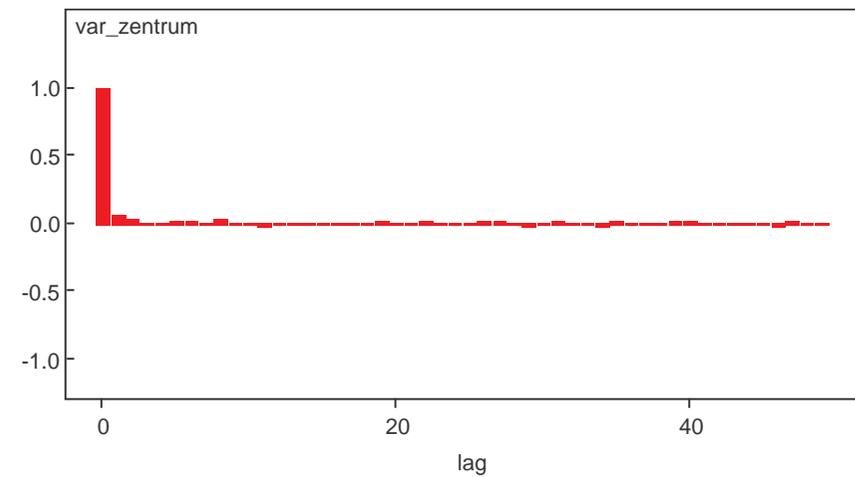
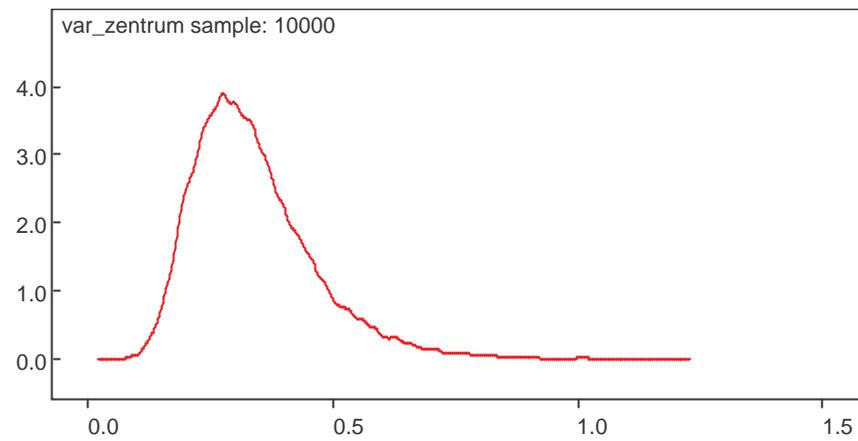
Covariate	Category	PROC NLMIXED $\beta$ (SE)	WinBUGS * $\beta$ (SE) **
Gender	Female	-0.161 (0.076)	-0.152 (0.073)
Age	$\geq$ 65 years	0.118 (0.060)	0.131 (0.057)
Histological type	SCLC	0.120 (0.071)	0.091 (0.068)
	Missing	-0.143 (0.120)	-0.140 (0.115)
Performance status (ECOG)	3-4	0.714 (0.114)	0.652 (0.110)
	Missing	0.145 (0.065)	0.158 (0.065)

\* 10.000 runs burn-in, 100.000 runs, thinning 1:10, non-informative priors

\*\* Posterior mean

## Results II: Random effects

Parameter	PROC NLMIXED	WinBUGS
$\sigma_h^2$	0.053 (0.037)	0.338 (0.125)



## Conclusion I

- A relative survival model for clustered responses can be easily defined by embedding Dickman's version of the Estève version into the class of generalized linear mixed models.
- Parameter estimation is straightforward, SAS PROC NLMIXED and WinBUGS can be used (besides others).
- For our data set fixed effects estimates in NLMIXED and WinBUGS did not differ, but random effects estimates did. This is compatible with our experience on other data sets.

## Conclusion II

- Coding complicated models in different software packages is a good idea and gives impression of robustness of results.
- Advantages PROC NLMIXED: ease of data handling, computation time
- Advantages WinBUGS: allows generalization to more random effects.

## References

1. Estève J, Benhamou E, Croasdale M, Raymond L. Relative survival and the estimation of net survival: Elements for further discussion. *Stat Med* 1990; 9:529-538.
2. Hakulinen T, Tenkanen L. Regression analysis of relative survival rates. *Appl Stat* 1987; 36:309-317.
3. Dickman PW, Sloggett A, Hills M, Hakulinen T. Regression Models for Relative Survival. *Stat Med* 2004; 23:51-64.